

# **New generation stellar model atmospheres**

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# **New generation stellar model atmospheres: why bother?**

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# Outline

- Why do we need stellar model atmospheres?
- What is stellar model atmosphere?
- What kind of model atmospheres are available today?
- New generation model atmospheres:
  - what are they and why bother?
  - if I want to use them, how do I do that?
- Final remarks

# Why do we need stellar model atmospheres?

## Why numerical simulations?

- In many cases: experiments technologically not possible or too expensive
- In particular in astronomy:
  - Objects far away => no *in situ* measurements
  - Extreme states of matter => often not achievable in the laboratory
  - Interpretation of observations – only with the help of theoretical models!
- Numerical simulations as important tool for the development and testing for physical theories



Sir Isaac Newton, apple tree, apple and the law of gravity.



# What is stellar model atmosphere?

What should a model atmosphere do?

- Wanted: simplest model that can account for all (relevant!) observations
- A model is valid within a certain scope and within certain assumptions  
⇒ Do not over-interpret!!

Feasibility

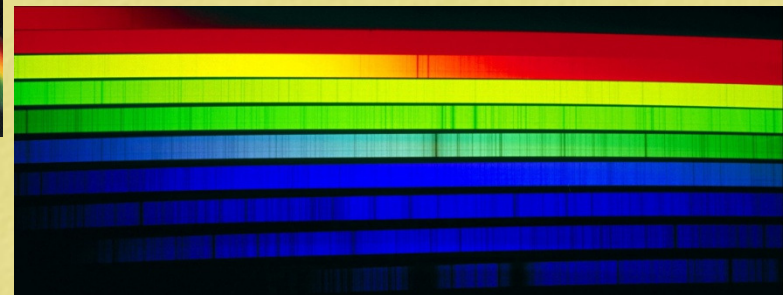
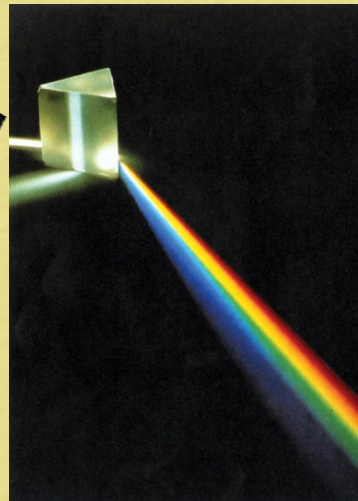
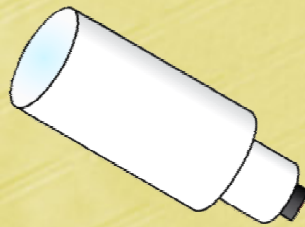
- Computational costs?!
- What is affordable? What is most important?  
⇒ Compromises, compromises, ...  
⇒ Simplifications, simplifications, ...



IT IS OK  
FOR ME  
TO HAVE  
EVERYTHING  
I WANT

# What is stellar model atmosphere?

From the problem to the model (I)

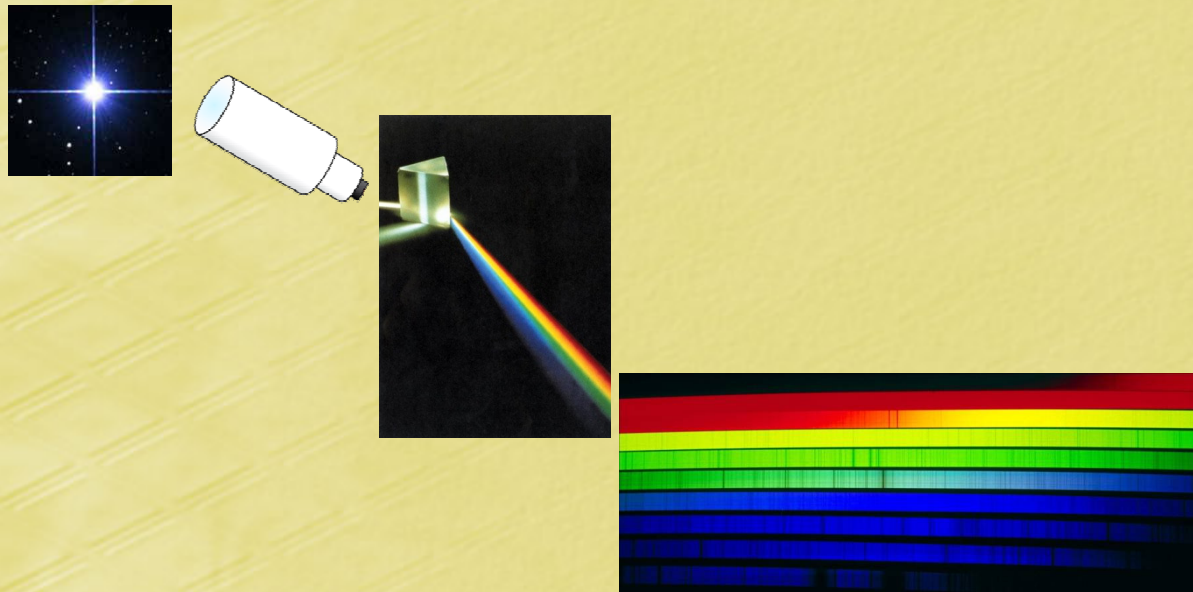




# What is stellar model atmosphere?

From the problem to the model (I)

- How to explain these observations?
- What are the physical processes behind?
- What do we need to realistically reproduce them in numerical model?



# What is stellar model atmosphere?

From the problem to the model (II)

- Formulating the relevant physical laws:
  - Which processes need to be included?
  - Time-dependent phenomenon?
  - Spatial structure?
    - How many spatial directions necessary? 1,2,3?
    - Can symmetries be exploited to simplify the modeling?

$$\frac{\partial \rho}{\partial t} = -\nabla \cdot (\rho \vec{v})$$

$$\frac{\partial \rho \vec{v}}{\partial t} = -\rho (\vec{v} \cdot \nabla) \vec{v} - \nabla P - \rho \vec{\nabla} \Phi$$

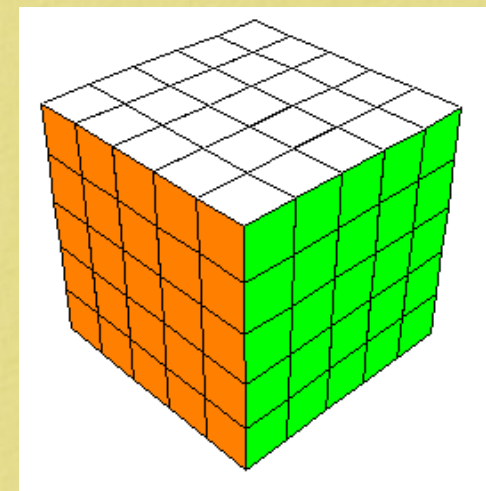
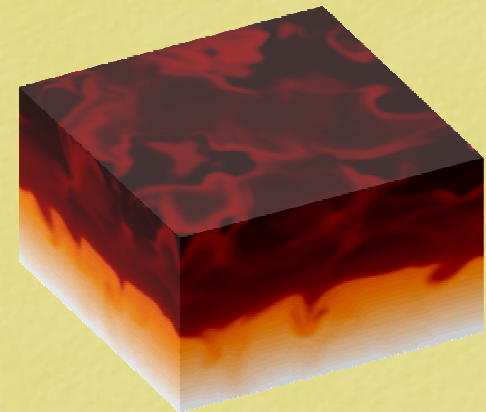
$$\frac{\partial \rho \varepsilon_{ik}}{\partial t} = -\nabla \cdot [(\rho \varepsilon_{ik} + P) \vec{v}] - \rho \vec{v} \cdot (\vec{\nabla} \Phi) + Q_{rad}$$



# What is stellar model atmosphere?

## From the problem to the model (III)

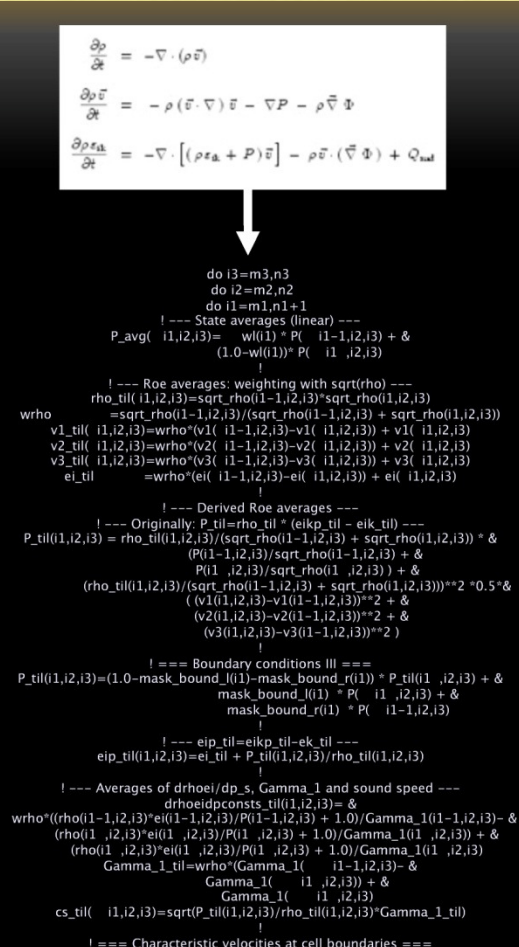
- Choice of the physical model size – the computational box:
  - How big must the computational box be to capture all important effects?
  - Example: fine-structure of the Sun: at least a few granules in each horizontal direction
- Discretization:
  - Solution of the physical equations at discrete grid location (or in grid cells)
  - Numerical grid:
    - geometry? boundary conditions?
    - adaptive mesh – more grid points where necessary?
    - how many grid points?



# What is stellar model atmosphere?

From the problem to the model (IV)

- Development of a computer code:
  - Needed: fast and numerically stable solution methods
  - Approximations and simplifications often necessary, for instance:
    - Pre-computed look-up tables for the equation of state
    - Multi-group opacities for the radiative transfer
    - And much more... ☺



The diagram illustrates the process of translating physical equations into a numerical code. At the top, three partial differential equations are shown in a white box:

$$\frac{\partial \rho}{\partial t} = -\nabla \cdot (\rho \vec{v})$$
$$\frac{\partial \rho \vec{v}}{\partial t} = -\rho (\vec{v} \cdot \nabla) \vec{v} - \nabla P - \rho \vec{\nabla} \Phi$$
$$\frac{\partial \rho \epsilon_A}{\partial t} = -\nabla \cdot [(\rho \epsilon_A + P) \vec{v}] - \rho \vec{v} \cdot (\vec{\nabla} \Phi) + Q_{\text{rad}}$$

A large white arrow points from these equations down to a Fortran code block. The code implements a numerical solution, including state averages, Roe averages, derived Roe averages, boundary conditions, and various physical quantities like sound speed and characteristic velocities.

```
do i3=m3,n3
do i2=m2,n2
do i1=m1,n1+1
! --- State averages (linear) ---
P_avg( i1,i2,i3)= w(i1)* P( i1-1,i2,i3) + &
(1.0-w(i1))* P( i1 i2,i3)
! --- Roe averages: weighting with sqrt(rho) ---
rho_til( i1,i2,i3)=sqrt_rho(i1-1,i2,i3)*sqrt_rho(i1,i2,i3)
= sqrt_rho(i1-1,i2,i3)/(sqrt_rho(i1-1,i2,i3) + sqrt_rho(i1,i2,i3))
wrho
v1_til( i1,i2,i3)=wrho*(v1( i1-1,i2,i3)-v1( i1,i2,i3)) + v1( i1,i2,i3)
v2_til( i1,i2,i3)=wrho*(v2( i1-1,i2,i3)-v2( i1,i2,i3)) + v2( i1,i2,i3)
v3_til( i1,i2,i3)=wrho*(v3( i1-1,i2,i3)-v3( i1,i2,i3)) + v3( i1,i2,i3)
ei_til
=wrho*(ei( i1-1,i2,i3)-ei( i1,i2,i3)) + ei( i1,i2,i3)
! --- Derived Roe averages ---
! --- Originally: P_til=rho_til * (eikp_til - eik_til) ---
P_til(i1,i2,i3) = rho_til(i1,i2,i3)/(sqrt_rho(i1-1,i2,i3) + sqrt_rho(i1,i2,i3)) * &
(P(i1-1,i2,i3)/sqrt_rho(i1-1,i2,i3) + &
P(i1 i2,i3)/sqrt_rho(i1 i2,i3)) + &
(rho_til(i1,i2,i3)/(sqrt_rho(i1-1,i2,i3) + sqrt_rho(i1,i2,i3)))**2 * 0.5 * &
((v1(i1,i2,i3)-v1(i1-1,i2,i3))**2 + &
(v2(i1,i2,i3)-v2(i1-1,i2,i3))**2 + &
(v3(i1,i2,i3)-v3(i1-1,i2,i3))**2 )
! === Boundary conditions III ===
P_til(i1,i2,i3)=(1.0-mask_bound_l(i1)-mask_bound_r(i1)) * P_til(i1 i2,i3) + &
mask_bound_l(i1) * P( i1 i2,i3) + &
mask_bound_r(i1) * P( i1-1,i2,i3)
! --- eip_til=eikp_til-ek_til ---
eip_til(i1,i2,i3)=ei_til + P_til(i1,i2,i3)/rho_til(i1,i2,i3)
! --- Averages of drhoei/dp_s, Gamma_1 and sound speed ---
drhoeidpconst_til(i1,i2,i3)= &
wrho*((rho(i1-1,i2,i3)*ei(i1-1,i2,i3)/P(i1-1,i2,i3) + 1.0)/Gamma_1(i1-1,i2,i3)- &
(rho(i1 i2,i3)*ei(i1 i2,i3)/P(i1 i2,i3) + 1.0)/Gamma_1(i1 i2,i3)) + &
(rho(i1 i2,i3)*ei(i1 i2,i3)/P(i1 i2,i3) + 1.0)/Gamma_1(i1 i2,i3)
Gamma_1_til=wrho*(Gamma_1( i1-1,i2,i3)- &
Gamma_1( i1 i2,i3)) + &
Gamma_1( i1 i2,i3)
cs_til( i1,i2,i3)=sqrt(P_til(i1,i2,i3)/rho_til(i1,i2,i3)*Gamma_1_til)
! === Characteristic velocities at cell boundaries ===
```



# What kind of model atmospheres are available today?

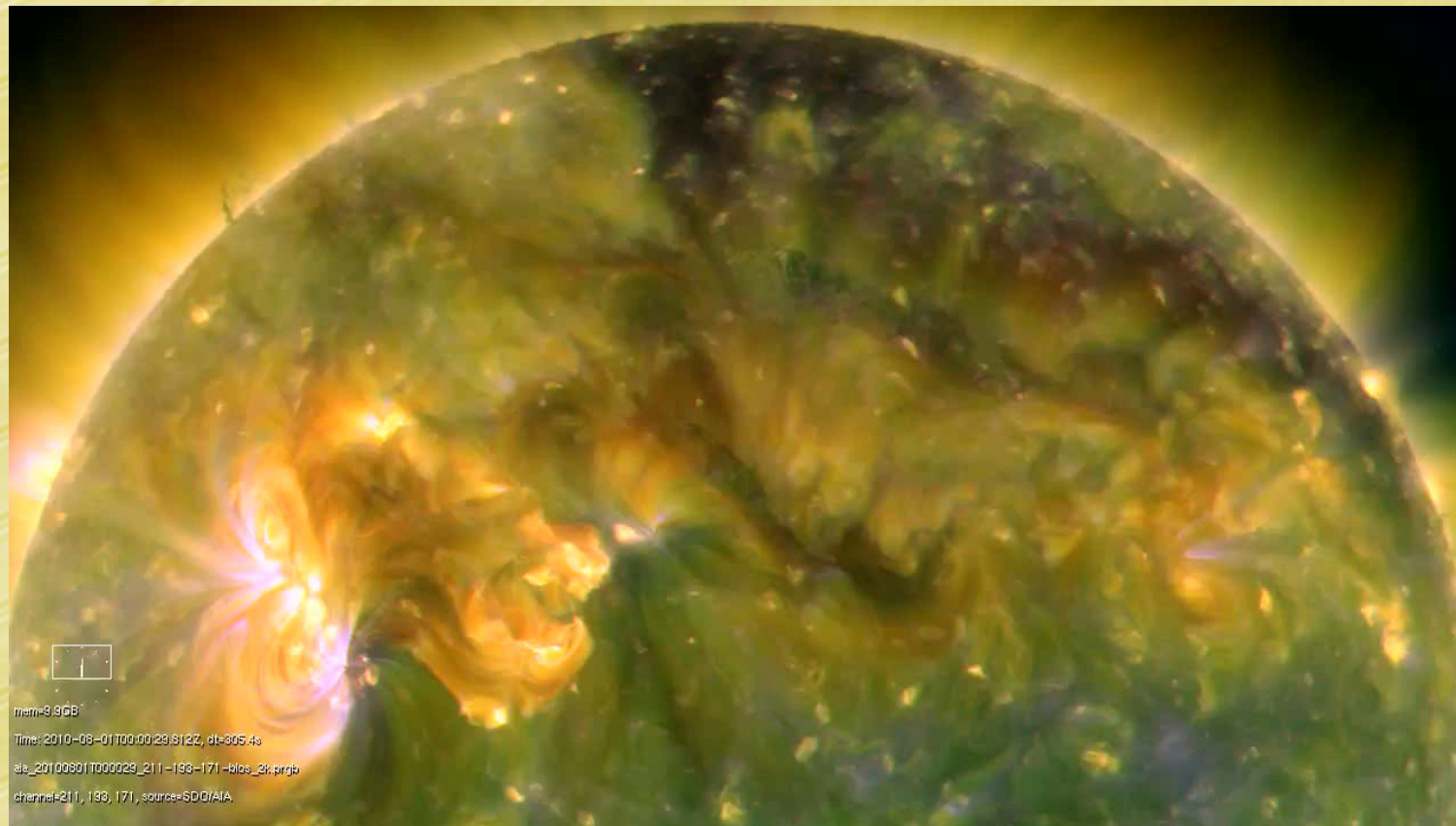
Classical approach: 1D stellar atmosphere models

- Computationally easily tractable:
  - ⇒ enable to include many physical processes in detail
  - ⇒ computation of large grids of stellar model atmospheres possible (ATLAS, MARCS, PHOENIX)
- Because of stationary and 1-dimensional nature – limitations, simplifications, and compromises:
  - simplified treatment of non-stationary phenomena (e.g., convection)
  - no possibility to account for 2D or 3D effects
    - ⇒ no spatial inhomogeneities, plane-parallel stratification, etc.

Nevertheless, standard workhorses today!

# What kind of model atmospheres are available today?

Real stars are not stationary nor one-dimensional!

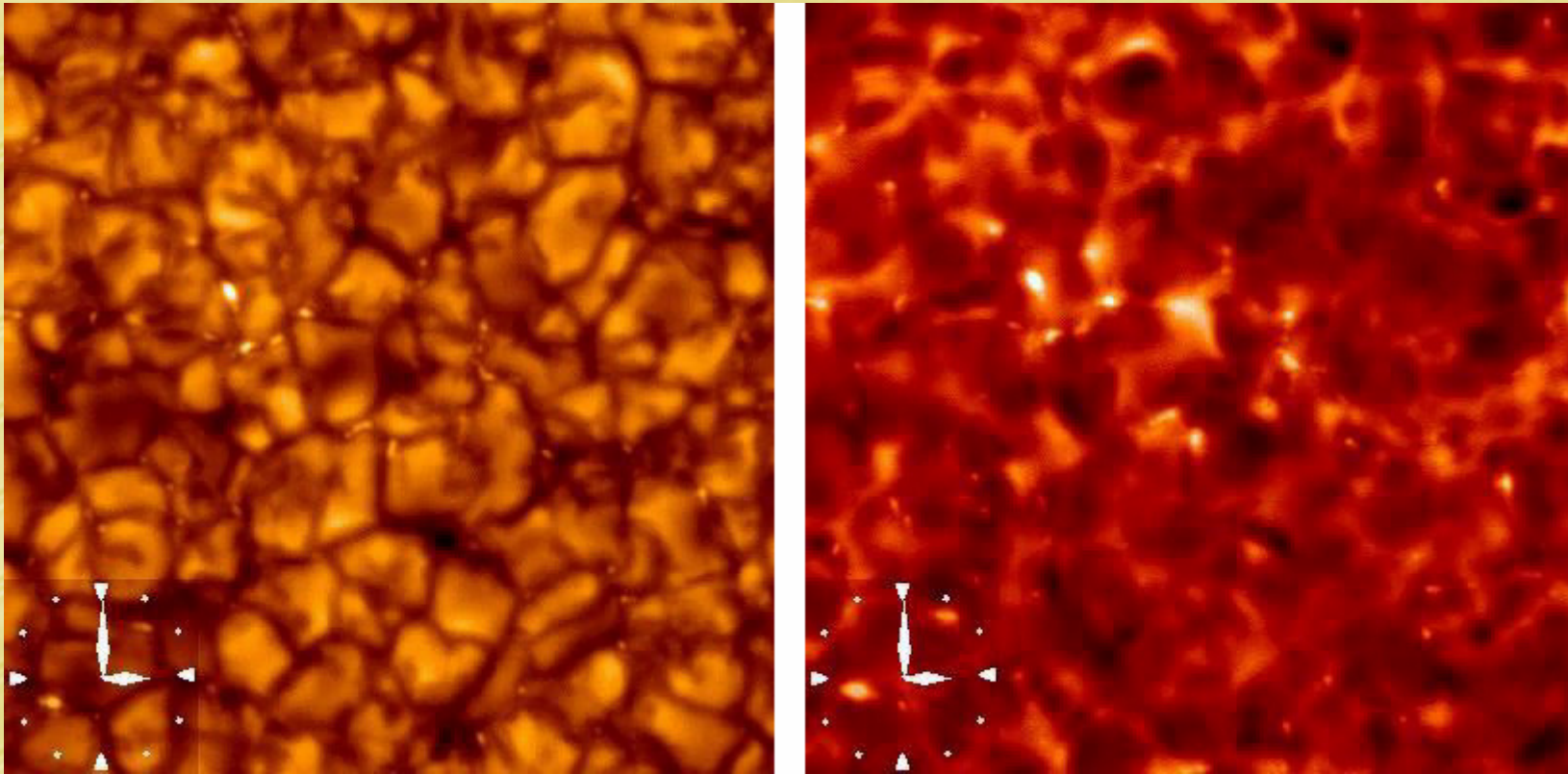


Solar Dynamics Observatory (SDO) view of the Sun.



# What kind of model atmospheres are available today?

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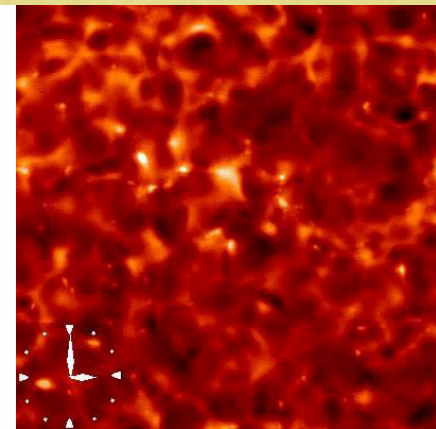
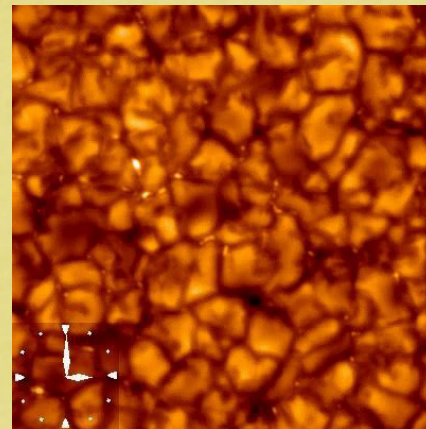
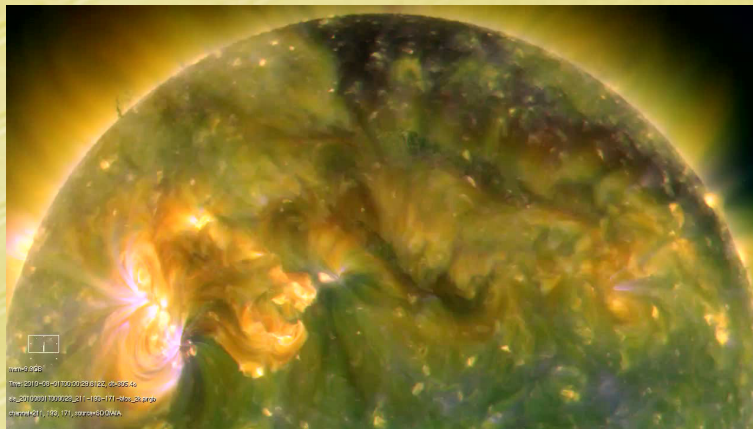


Quiet Sun: in the G-band (430 nm, left) and Ca II H band (397 nm, right; SOT/Hinode).

# What kind of model atmospheres are available today?

Real stars are neither stationary nor one-dimensional!

- High-resolution observations of the Sun demonstrate: variability on a multitude of spatial and temporal scales!
- 3D hydrodynamical approach necessary!

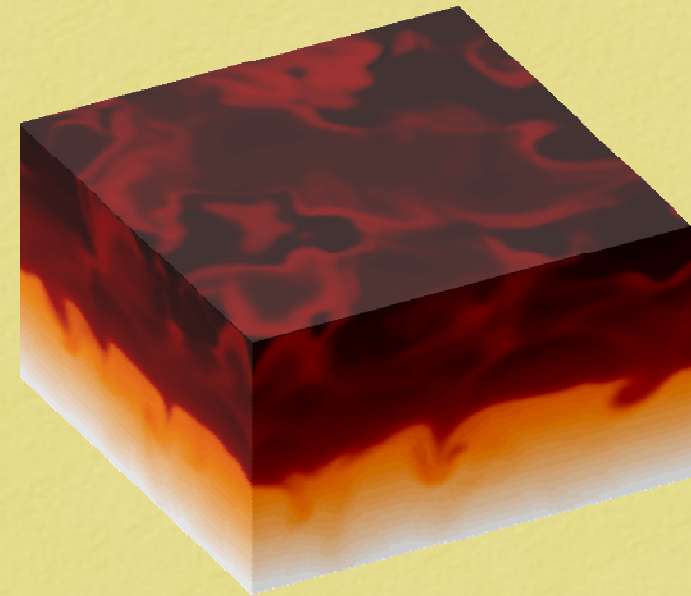




# What kind of model atmospheres are available today?

New generation stellar model atmospheres: 3D hydrodynamical models

- Numerical solution of:
  - (magneto-)hydrodynamics
  - radiative transfer
  - “realistic” equation of state and opacities
  - advancing simulation in time step by step
  - result: time sequence of 3D snapshots (containing primary variables, e.g.,  $\rho$ ,  $e$ ,  $v_x$ ,  $v_y$ ,  $v_z$ ) and auxiliary data

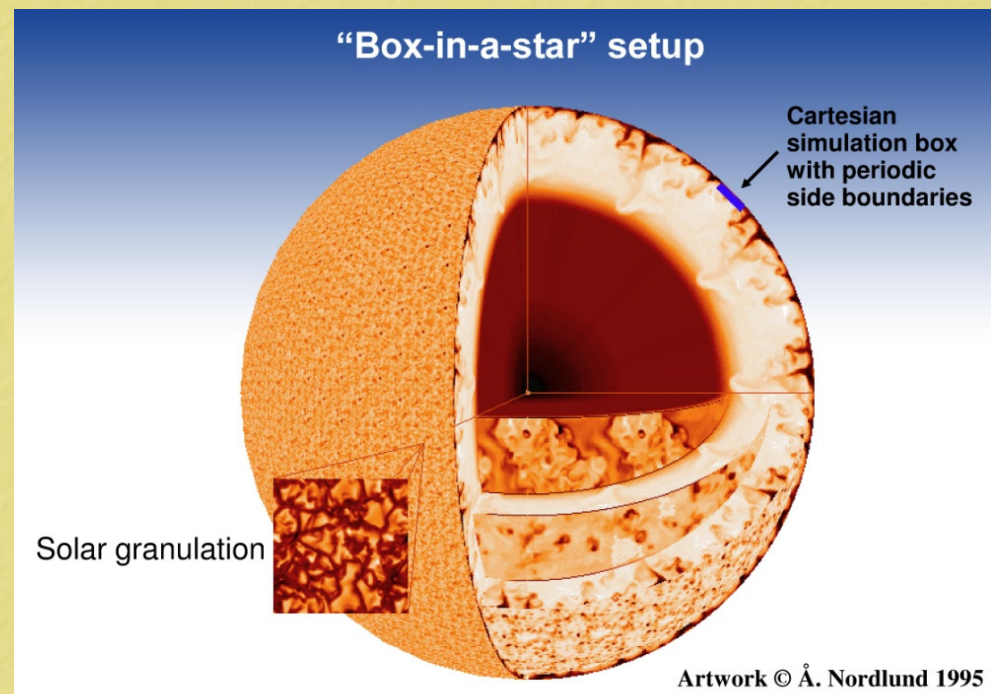


Temperature distribution in the 3D hydrodynamical model atmosphere (Wdemayer-Boehm et al. 2007).

# What kind of model atmospheres are available today?

What is different with respect to classical 1D models?

- Solution of 3D radiation-hydrodynamics equations in 3D Cartesian space



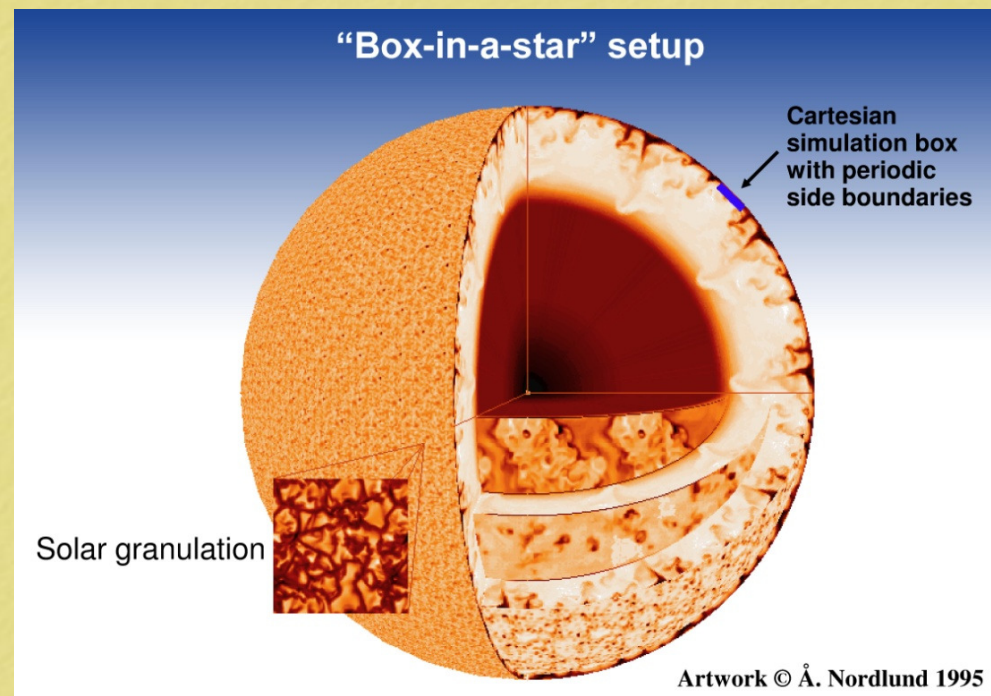
Schematic model of Solar granulation. Blue bar indicates the approximate position of the 3D RHD model simulation box (after M. Steffen).



# What kind of model atmospheres are available today?

What is different with respect to classical 1D models?

- Solution of 3D radiation-hydrodynamics equations in 3D Cartesian space
- No *apriori* assumptions about stellar velocity fields

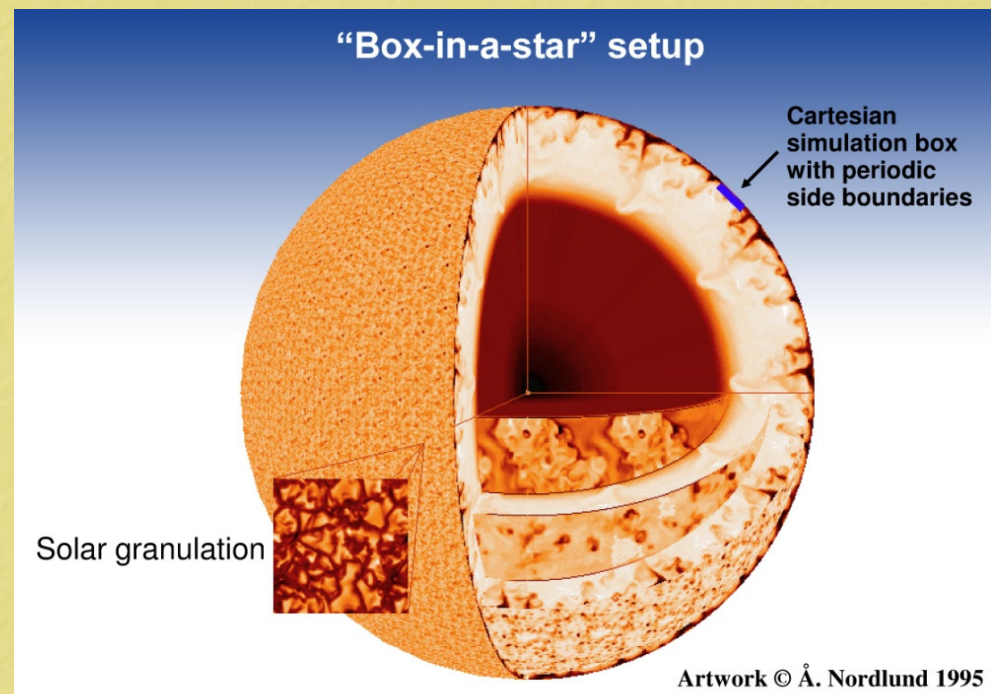


Schematic model of Solar granulation. Blue bar indicates the approximate position of the 3D RHD model simulation box (after M. Steffen).

# What kind of model atmospheres are available today?

What is different with respect to classical 1D models?

- Solution of 3D radiation-hydrodynamics equations in 3D (Cartesian) space
- No *a priori* assumptions about stellar velocity fields
- Significantly higher computational costs: simplifications with respect to 1D
- Both global and local models

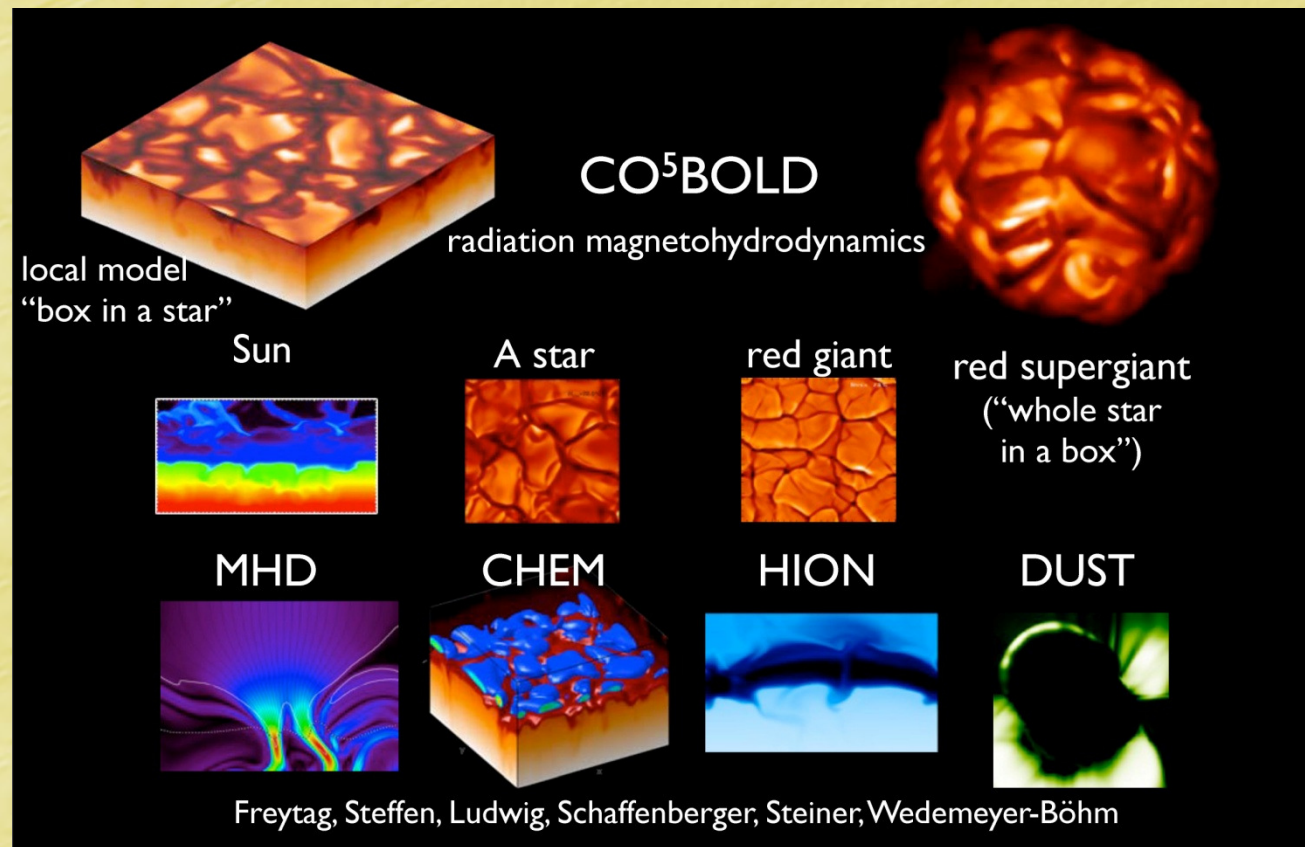


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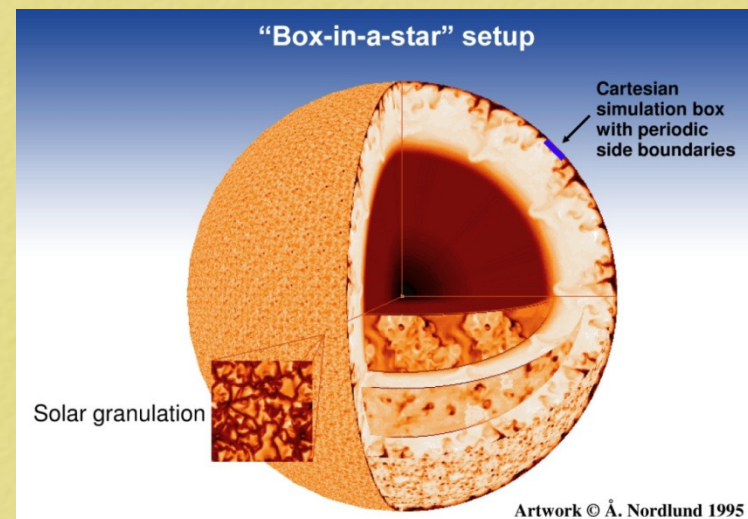
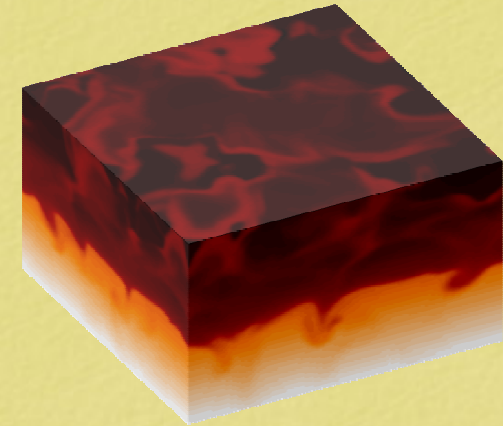
Example: CO<sup>5</sup>BOLD radiation magnetohydrodynamics model atmosphere code



# What kind of model atmospheres are available today?

Example: CO<sup>5</sup>BOLD model atmosphere code

- Numerical solution of:
  - radiation magnetohydrodynamics (LTE, opacity binning)
  - “realistic” equation of state and opacities (MARCS opacities)
  - result: time sequence of 3D snapshots (containing primary variables,  $\rho$ ,  $e$ ,  $v_x$ ,  $v_y$ ,  $v_z$ ,  $B_x$ ,  $B_y$ ,  $B_z$ ) and auxiliary data
- Both local (“box in a star”) and global (“star in a box”) model atmospheres



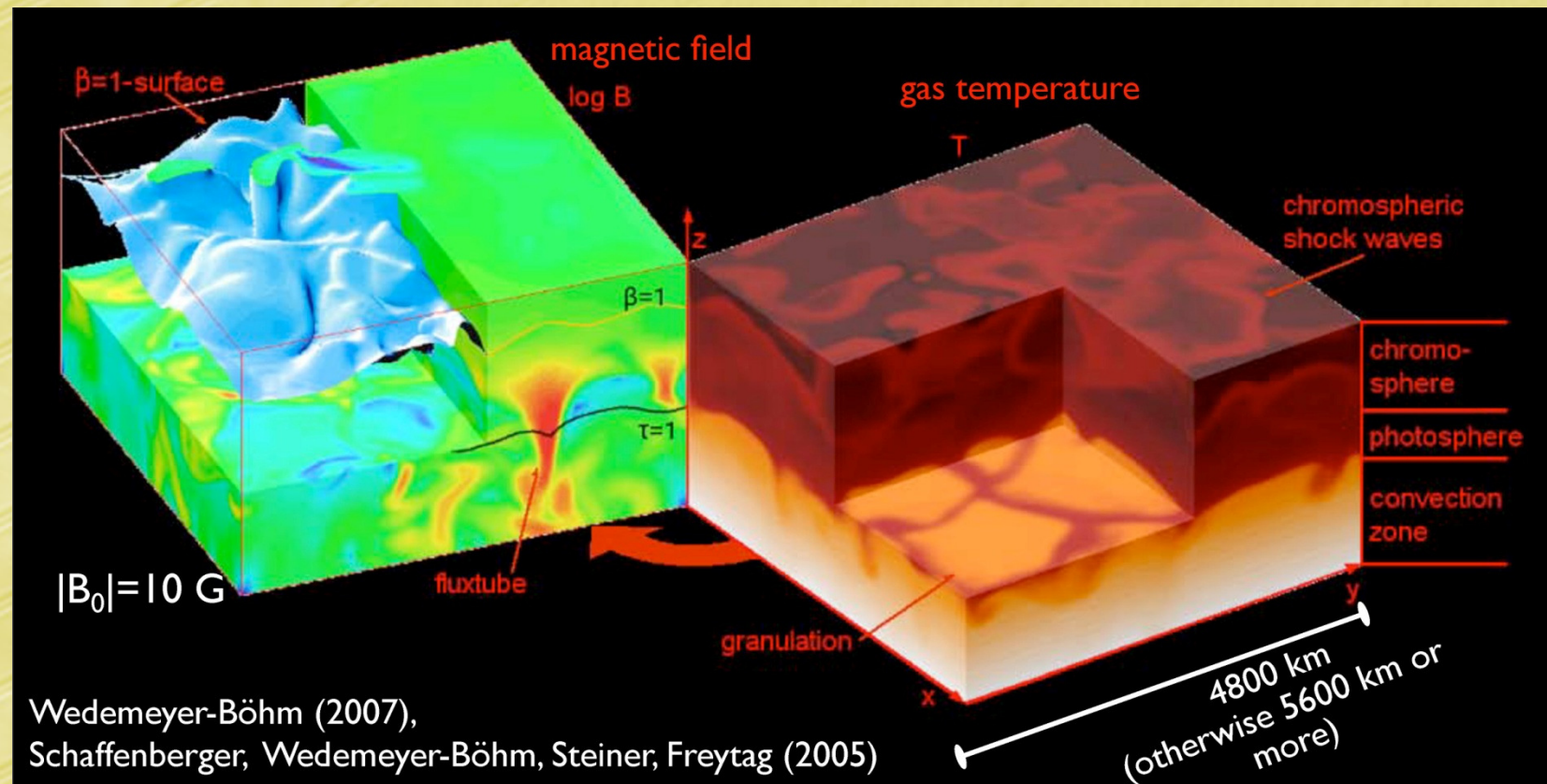
Schematic model of Solar granulation. Blue bar indicates the approximate position of the 3D RHD model simulation box.



# What kind of model atmospheres are available today?

## Local CO<sup>5</sup>BOLD models

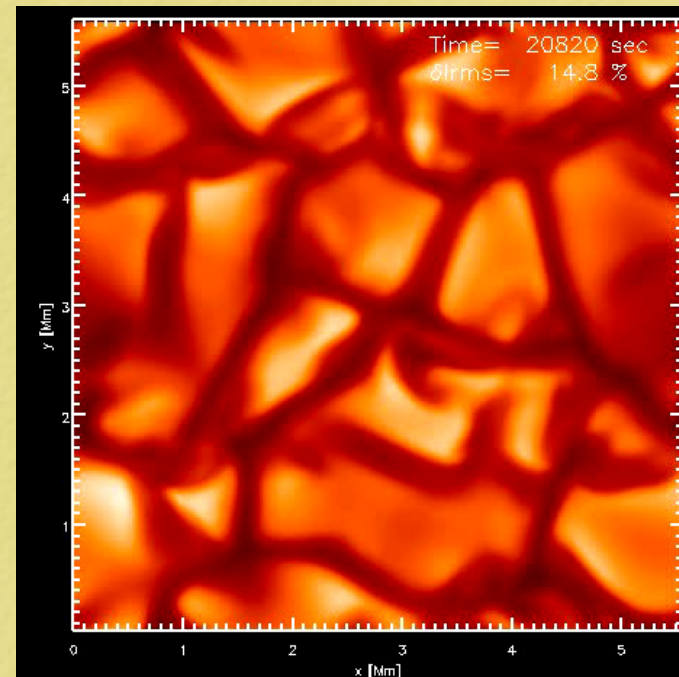
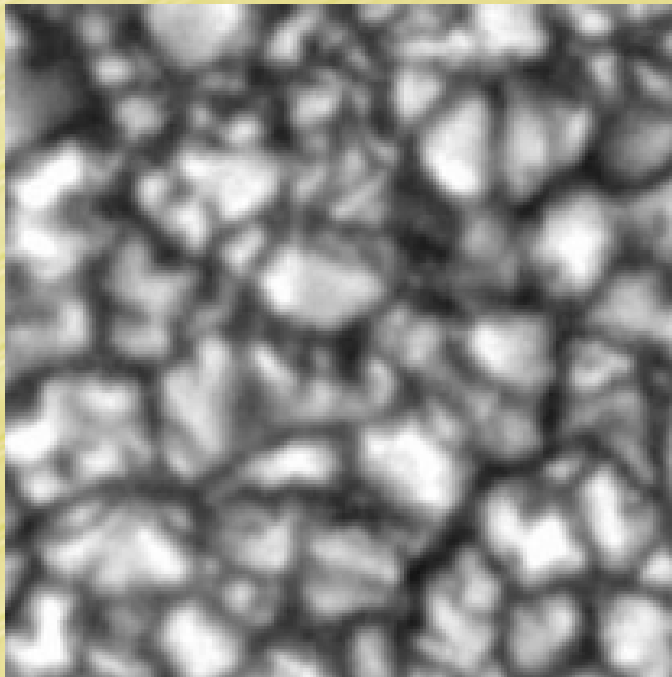
- Top of convection zone, photosphere, and chromosphere



# New generation stellar model atmospheres: why bother?

What can the 3D hydrodynamical models provide beyond the classical 1D view? Example I

- Effects of radiation and velocity fields on the atmospheric structures: stellar granulation



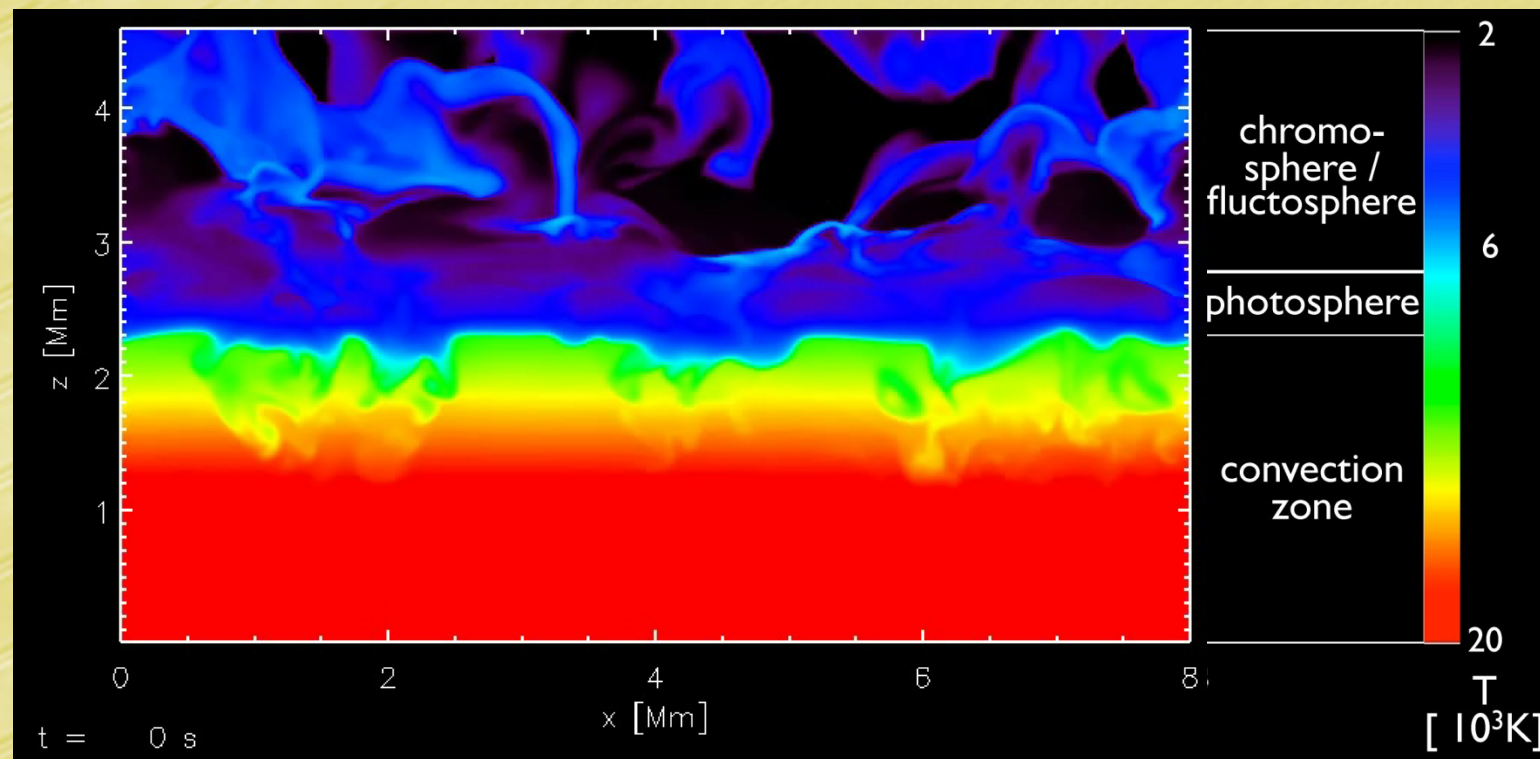
Granulation in the solar atmosphere, observations (left) and 3D hydrodynamical CO5BOLD model (right).



# New generation stellar model atmospheres: why bother?

What can the 3D hydrodynamical models provide beyond the classical 1D view? Example II

- 3D hydrodynamical view of stellar photospheres and chromospheres

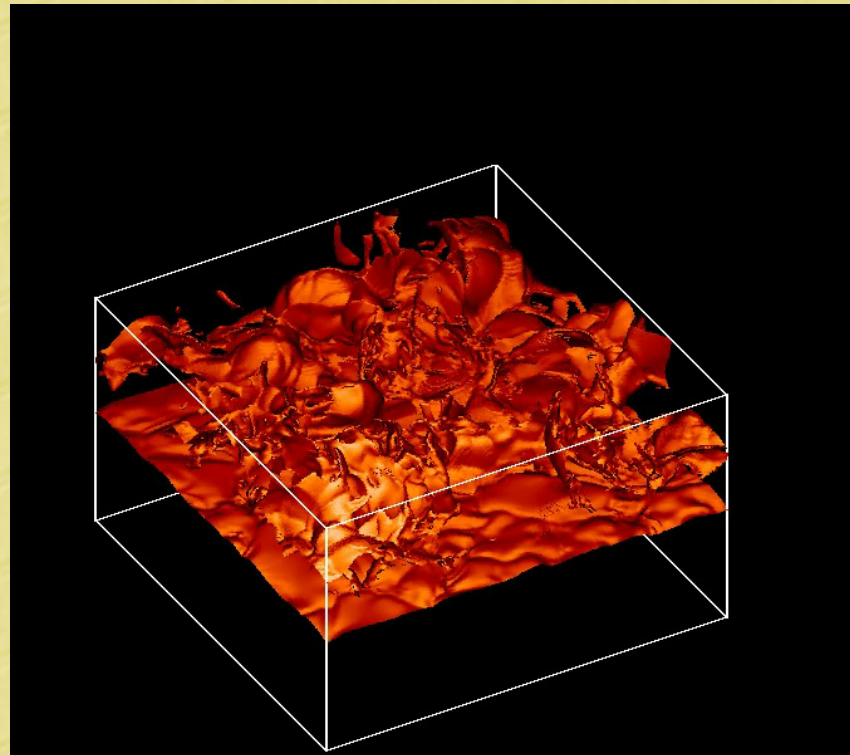


3D hydrodynamical CO5BOLD model of the solar atmosphere (Wedemeyer-Böhm, in prep.).

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- 3D hydrodynamical view of stellar photospheres and chromospheres



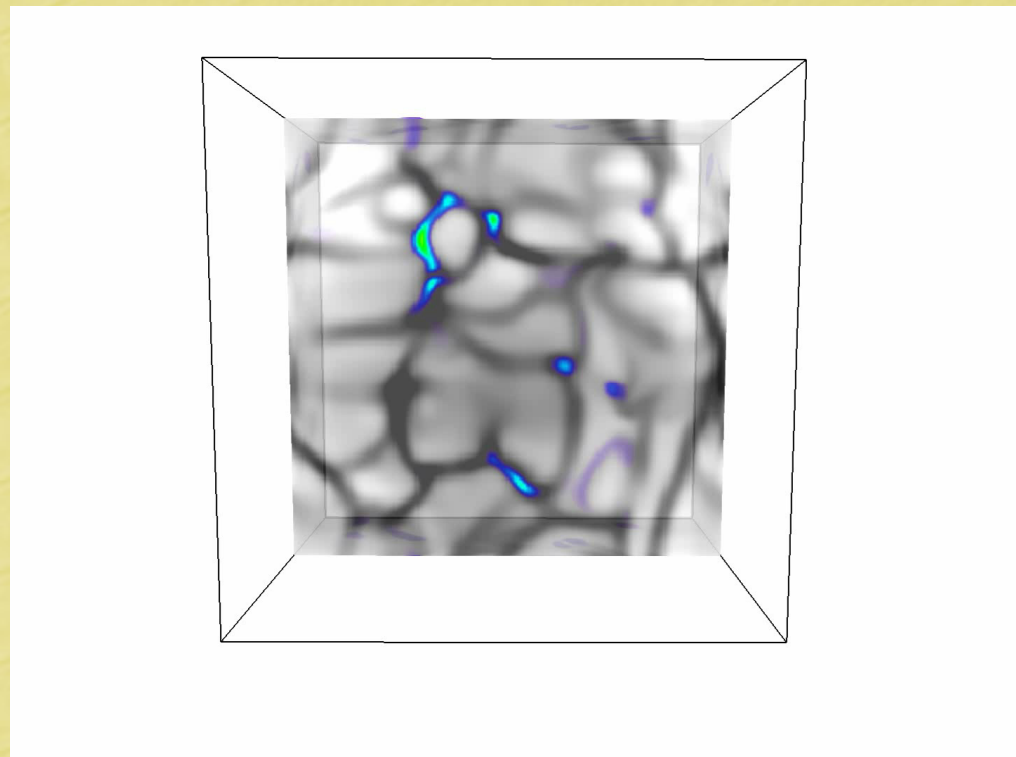
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# New generation stellar model atmospheres: why bother?

What can the 3D hydrodynamical models provide beyond the classical 1D view? Example III

- Evolution of magnetic structures in stellar atmospheres

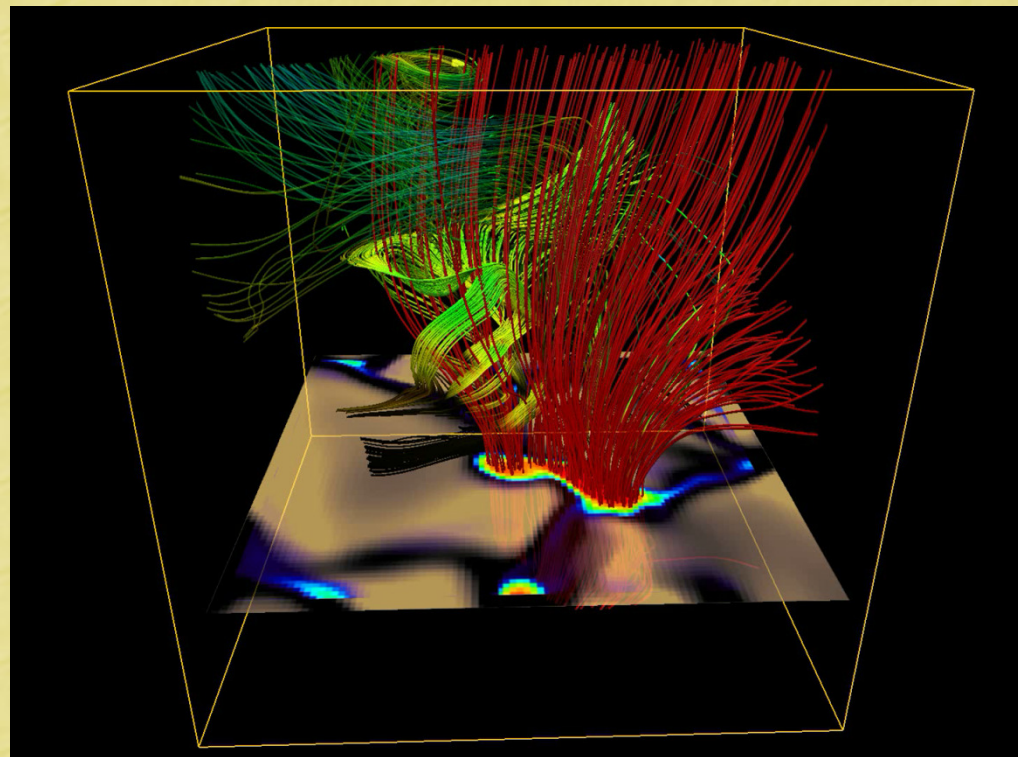


Magnetic structures in the 3D hydrodynamical CO5BOLD model of the solar atmosphere (Wedemeyer-Böhm, in prep.).

# New generation stellar model atmospheres: why bother?

What can the 3D hydrodynamical models provide beyond the classical 1D view? Example III

- Evolution of magnetic structures in stellar atmospheres



Magnetic structures in the 3D hydrodynamical CO5BOLD model of the solar atmosphere (Wedemeyer-Böhm, in prep.).



# New generation stellar model atmospheres: why bother?

What can the 3D hydrodynamical models provide beyond the classical 1D view?

## Summary

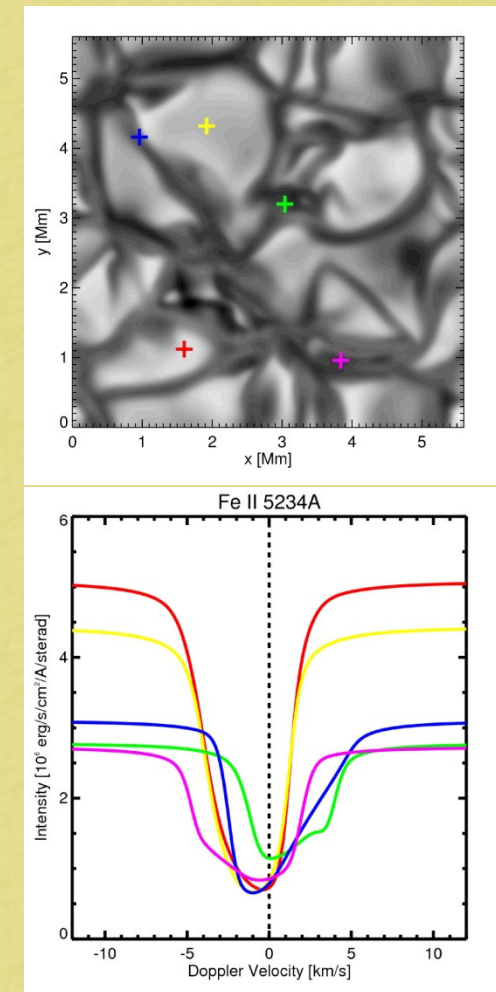
- Effects of radiation and velocity fields on the atmospheric structures
- 3D hydrodynamical view of stellar photospheres and chromospheres
- Evolution of magnetic structures in stellar atmospheres

**⇒ Implications on the observable properties of real stars: spectra, photometric colors, radial velocities and so on!!**

# New generation stellar model atmospheres: why bother?

## 3D hydrodynamical effects in stellar atmospheres

- Implications on the spectral line formation:
  - Variations in line strengths, widths, shifts, asymmetries across granulation pattern
  - Non-linearities cause net effects in disk-integrated light



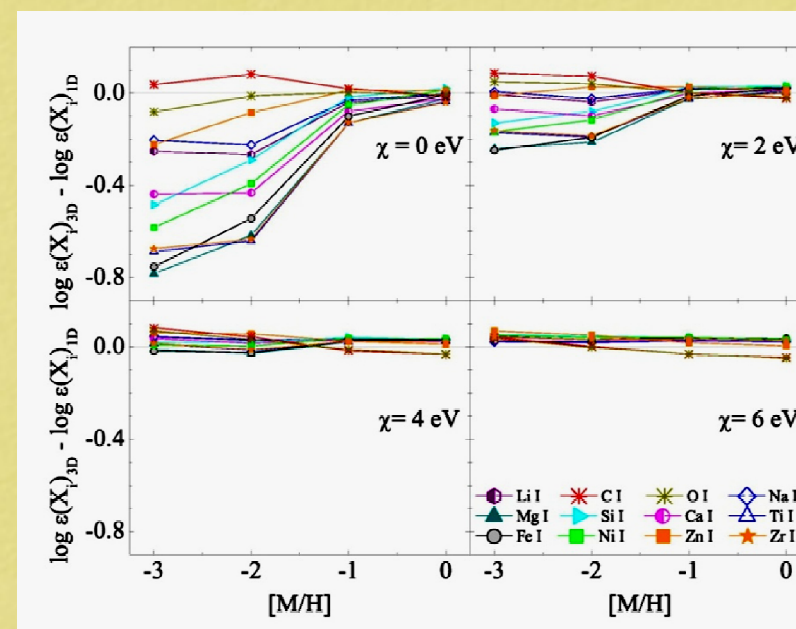
Top: surface granulation in the 3D hydrodynamical CO5BOLD model of the Sun.  
Bottom: shapes of Fe II lines formed at different locations in solar atmosphere.



# New generation stellar model atmospheres: why bother?

## 3D hydrodynamical effects in stellar atmospheres

- Implications on the spectral line formation:
  - Differences in the abundances derived with classical 1D and 3D hydrodynamical model atmospheres

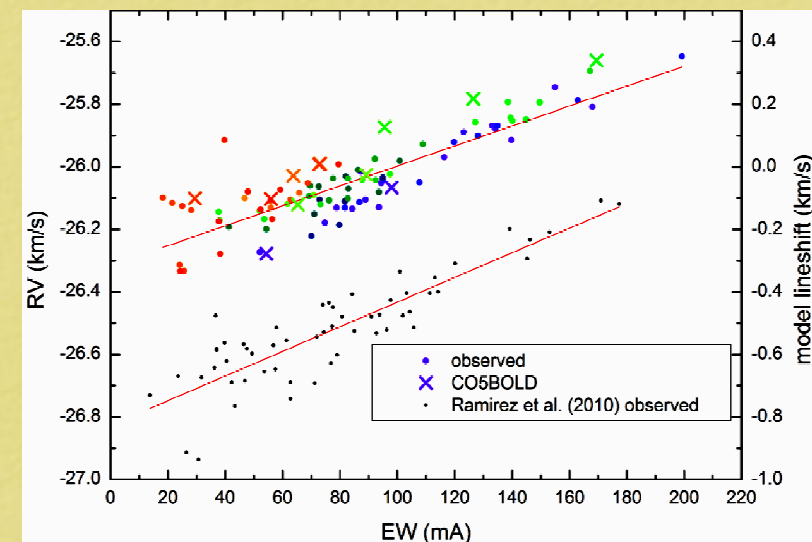


3D – 1D abundance corrections for various neutral atoms characterized by various excitation potentials, plotted versus metallicity (Dobrovolskas et al. 2012, in prep.).

# New generation stellar model atmospheres: why bother?

## 3D hydrodynamical effects in stellar atmospheres

- Implications on the spectral line formation:
  - Differences in the abundances derived with classical 1D and 3D hydrodynamical model atmospheres
  - Spectral line shifts: largest in case of weakest spectral lines



Measured (dots) and calculated (crosses, COBOLD models) line shifts in the atmosphere of the metal-poor giant HD 122563 (Klevas et al. 2012, in prep.).



# New generation stellar model atmospheres: why bother?

## 3D hydrodynamical effects in stellar atmospheres

- Implications on the spectral line formation:
  - Differences in the abundances derived with classical 1D and 3D hydrodynamical model atmospheres
  - Spectral line shifts: largest in case of weakest spectral lines
  - Different radial velocity shifts for different stars

Stellar type	$T_{\text{eff}}$ [K]	$\log g$	[Fe/H]	Mass [ $M_{\odot}$ ]	$R_{\star}$ [ $R_{\odot}$ ]	$\Delta\lambda_{\text{FeI}}$ [km.s <sup>-1</sup> ]	$\Delta\lambda_{\text{CaII}}$ [km.s <sup>-1</sup> ]	Ref.	Symbol
Local simulations with STAGGER-CODE									
K giant	4700	2.2	0.0	...	...	-0.36	+0.29	[8]	●
K giant	4720	2.2	-1.0	...	...	-0.45	+0.23	[8]	▲
K giant	5035	2.2	-2.0	...	...	-0.58	+0.25	[8]	▼
K giant	5130	2.2	-3.0	...	...	-0.28	+0.31	[8]	◆
K giant	4630	1.6	-3.0	...	...	-0.22	+1.55	[9]	■
F star	6500	4.0	0.0	...	...	-0.75	+3.4	[10]	★
Global simulations with CO <sup>5</sup> BOLD									
RSG	3430	-0.35	0.0	12	846	+0.75	-1.89	[5]	●
RSG	3660	0.02	0.0	6	386	+2.80	-7.95	[5]	★

Radial velocity shifts for Fe I and Ca II lines predicted by the 3D hydrodynamical models for different types of stars (Chiavassa et al. 2011).

# New generation stellar model atmospheres: why bother?

3D hydrodynamical effects in stellar atmospheres

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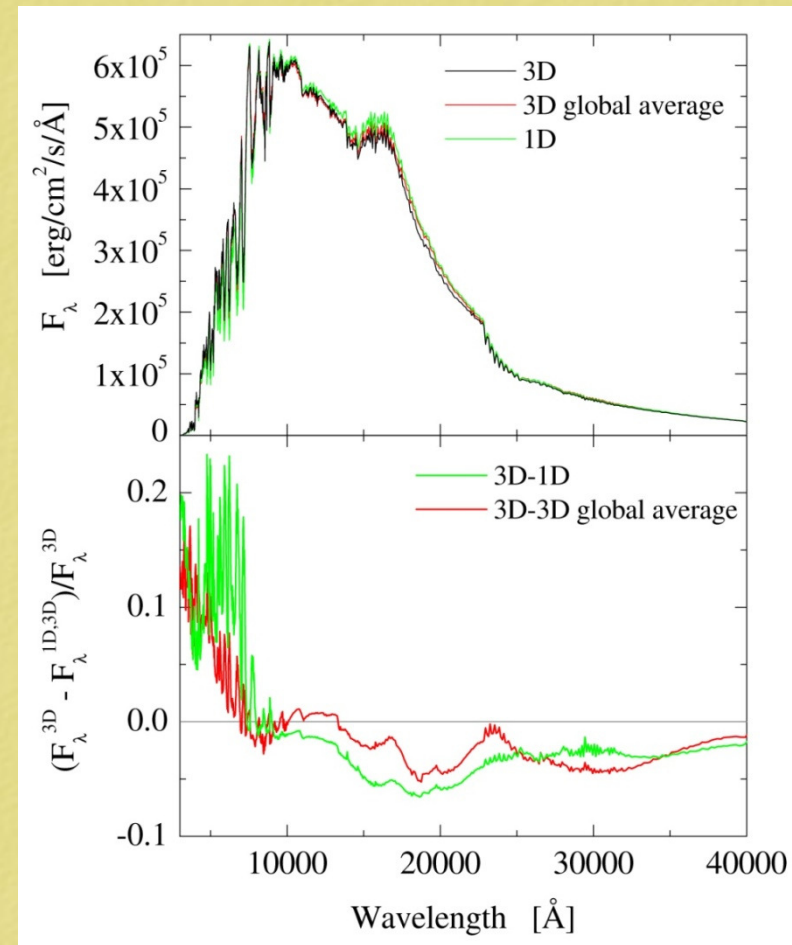
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K giant	5130	2.2	-3.0	...	...	-0.28	+0.31	[8]	◆
K giant	4630	1.6	-3.0	...	...	-0.22	+1.55	[9]	■
F star	6500	4.0	0.0	...	...	-0.75	+3.4	[10]	★
Global simulations with CO <sup>5</sup> BOLD									
RSG	3430	-0.35	0.0	12	846	+0.75	-1.89	[5]	●
RSG	3660	0.02	0.0	6	386	+2.80	-7.95	[5]	★

Radial velocity shifts for Fe I and Ca II lines predicted by the 3D hydrodynamical models for different types of stars (Chiavassa et al. 2011).

# New generation stellar model atmospheres: why bother?

## 3D hydrodynamical effects in stellar atmospheres

- Implications on the global trends in stellar spectra:
  - 3D model produces more flux than its 1D counterpart in the blue spectral region and less in the red/near-infrared



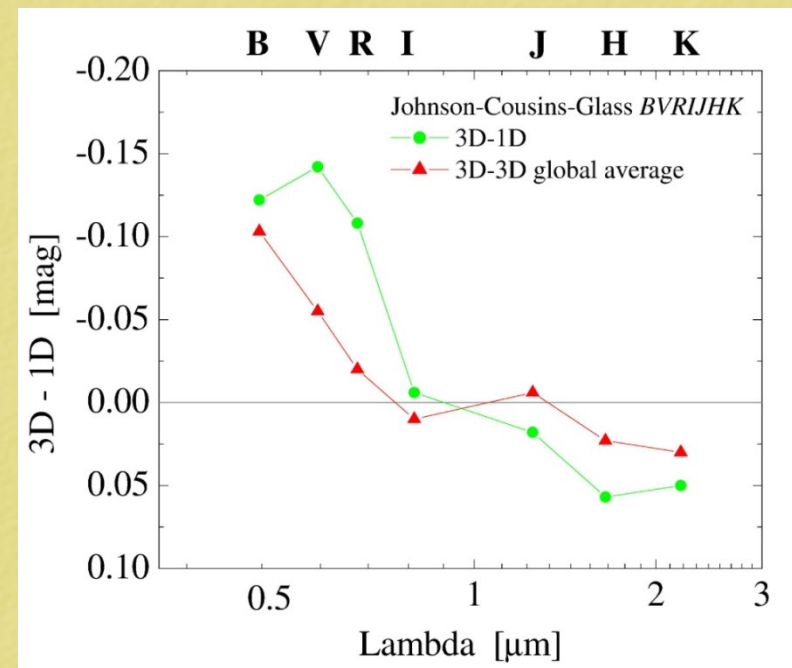
Top: Spectral energy distributions of the 3D (black),  $\langle 3D \rangle$  global average (red) and 1D (green) models of red giant. Bottom: differences between the spectral energy distributions: 3D–1D (green) and 3D –  $\langle 3D \rangle$  (red) (Kucinkas et al, in prep.).



# New generation stellar model atmospheres: why bother?

## 3D hydrodynamical effects in stellar atmospheres

- Implications on the global trends in stellar spectra:
  - 3D model produces more flux than its 1D counterpart in the blue spectral region and less in the red/near-infrared
  - Differences in the photometric colors predicted with classical 1D and 3D hydrodynamical model atmospheres

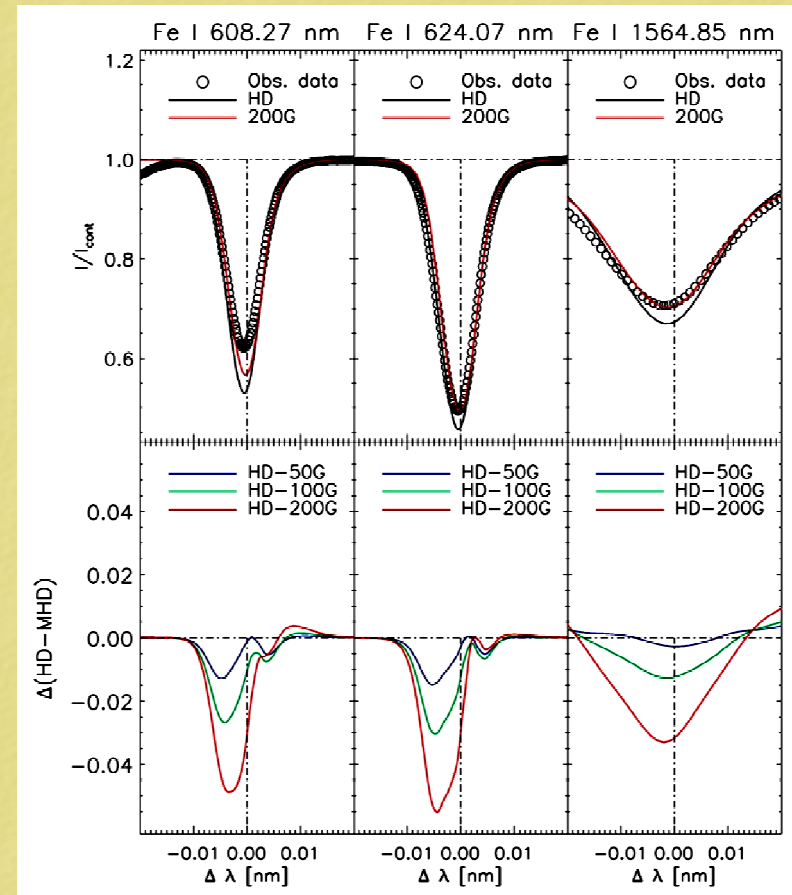


Differences in the photometric colors: 3D–1D (green) and 3D–3D\_global\_average (red) (Kucinkas et al., in prep.).

# New generation stellar model atmospheres: why bother?

## 3D magnetohydrodynamical effects in stellar atmospheres

- MHD models of solar atmosphere :
  - Noticeable differences in Fe I line strengths predicted with the 3D MHD and pure 3D hydrodynamical model atmospheres
  - Better agreement of 3D MHD Fe I line profiles with observations



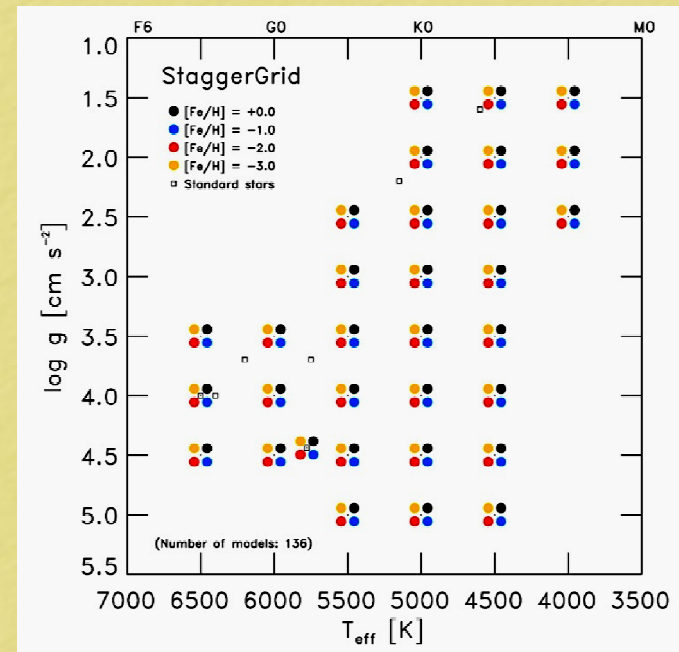
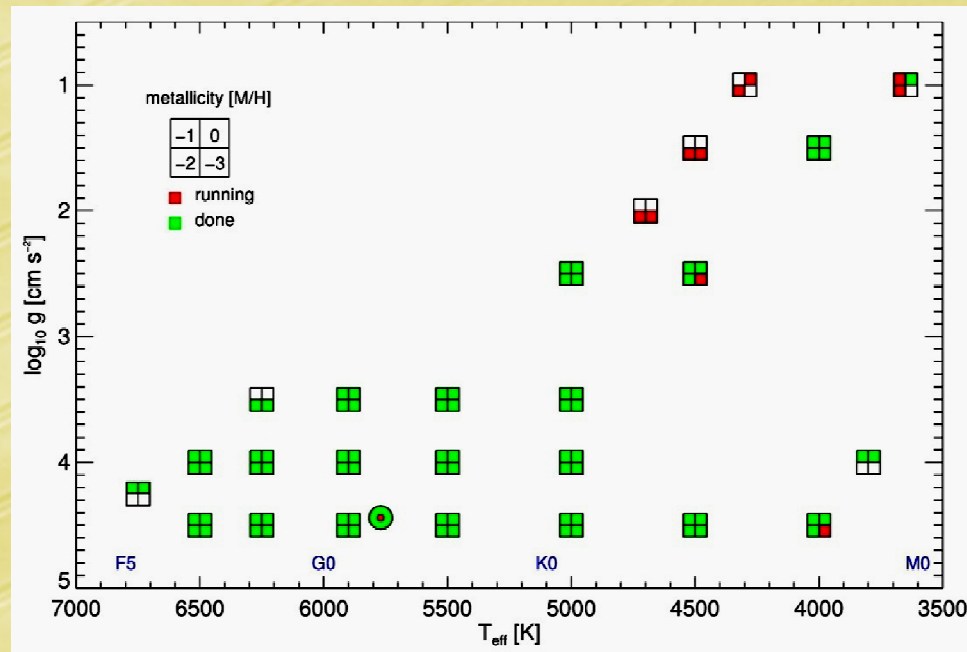
Top: observed (dots), 3D hydrodynamical (black lines), and 3D MHD (red lines) profiles of Fe I lines in the solar spectrum. Bottom: differences between the observed and theoretical line profiles (Fabbian et al. 2010).



# New generation stellar model atmospheres: user's perspective

## 3D stellar atmospheres for your work

- Grids of 3D model atmospheres are starting to appear
- Advice on possible use available from the modelers!



CO5BOLD (left, Ludwig et al. 2009) and STAGGER (right, Collet et al. 2011) grids of 3D hydrodynamical model atmospheres.

# New generation stellar model atmospheres: final remarks

- 3D (magneto)hydrodynamical model atmospheres are becoming available  
⇒ **use them!**
- 3D (magneto)hydrodynamical model atmospheres are still experimental  
⇒ **use with caution!!**
- ANY model atmosphere is based on a (LARGE!!) number of different assumptions, simplifications, and compromises  
⇒ **do not over-interpret!!!**



**THANK YOU!**

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# What kind of model atmospheres are available today?

Other 3D hydrodynamical stellar model atmospheres

- STAGGER code (REFERENCES!!)
  - BIFROST code (former Oslo-STAGGER code; REFERENCES!!)
  - MURAM code
  - .....
- ⇒ enable to include many physical processes in detail
- ⇒ computation of large grids of stellar model atmospheres possible (ATLAS, MARCS, PHOENIX)



